Leave No Context Behind: Efficient Infinite Context Transformers with Infini-attention

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## Attention

(Self)-attention is the main component of the transformer architecture. Given a input sequence  $x \in \mathbb{R}^{L \times d_{\text{model}}}$  a single head, vanilla self-attention is computed as follows:

1. Compute query, key, value with the trainable weights  $W_q, W_k \in \mathbb{R}^{d_k \times d_{\text{model}}}$ , and  $W_v \in \mathbb{R}^{d_v \times d_{\text{model}}}$  by

$$Q = xW_q, \quad K = xW_k, \quad V = xW_v$$

2. Compute the *mask* by

$$\tilde{A}_{\rm dot} = {\rm softmax} \left( \frac{QK^{\rm T}}{\sqrt{d_{\rm model}}} \right)$$

3. Compute the attention

$$A_{\mathsf{dot}} = \tilde{A}_{\mathsf{dot}} V$$

Note that computing  $\tilde{A}_{dot}$  requires  $\mathcal{O}(L^2)$  computation and memory complexity. Informally, since each element of sequence is compared with every other element, the amount of computation and memory increase quadratic to the length of sequence. To overcome this drawback:

Within attention mechanism: use window size N < L for attention.

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Use alternatives: e.g. State Space Model (SSM)

## Problem with Attention

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Within attention mechanism: use window size N < L for attention.

 $\Rightarrow$  Loss global context!

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Use alternatives: e.g. State Space Model (SSM)

## Infini-attention

This paper proposes *Infini-attention* to capture both local and global context states.

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### **Compressive Memory**

**Memory retrieval (query).** Given a memory  $M_{s-1} \in \mathbb{R}^{d_k \times d_v}$ , compressed memory  $A_{\text{mem}}$  is computed by

$$A_{\rm mem} = \frac{\sigma(Q)M_{s-1}}{\sigma(Q)z_{s-1}},$$

where  $Q \in \mathbb{R}^{L \times d_k}$  is shared with  $A_{dot}$  and  $z_{s-1}$  is the normalization term.

Memory update (key-value).

$$M_s = M_{s-1} + \sigma(K)^{\mathsf{T}} \left( V - \frac{\sigma(Q)M_{s-1}}{\sigma(Q)z_{s-1}} \right)$$
$$z_s = z_{s-1} + \sum_{t=1}^N \sigma(K_t)$$

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## **Compressive Memory**

#### **High-level interpretation**

Local information: Q, K, V computed for A<sub>dot</sub>
 ⇒ A<sub>dot</sub> queries for given sequence x to the current local KV
Global information: M<sub>s</sub> containing key-value entries
 ⇒ A<sub>mem</sub> queries for given sequence x to the global KV

## Infini-attention

 $A = \mathsf{sigmoid}(\beta) \odot A_{\mathsf{mem}} + (1 - \mathsf{sigmoid}(\beta)) \odot A_{\mathsf{dot}}$ 

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#### Task: PG19, Arxiv-math

#### ▶ N = 2048, input sequence length 32768

Model	Memory size (comp.)	XL cache	Segment length	PG19	Arxiv-math
Transformer-XL	50M (3.7x)	2048	2048	11.88	2.42
Memorizing Transformers	183M (1×)	2048	2048	11.37	2.26
RMT	2.5M (73x)	None	2048	13.27	2.55
Infini-Transformer (L)	1.6M (114×)	None	2048	9.65	2.24
Infini-Transformer (L + D)	1.6M (114×)	None	2048	9.67	2.23

Table 1: Comparison of different long-context language modeling.

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Two types of heads

- Specialized heads: gating score ≈ 0, 1
- Mixer heads: gating score  $\approx 0.5$
- ► Each layer has at least one short-range head (gating score ≈ 0)

	0.5	0.7	0.7	0.7	0.5	0.0	0.1	0.6
	0.0	0.0	0.0	0.6	0.0	0.2	0.0	0.3
	0.3	0.0	0.9	0.7	0.5	0.7	0.0	0.7
	0.8	0.8	0.4	0.0	0.7	0.0	0.3	0.0
	0.0	0.0	0.3	0.2	0.1	0.0	0.5	0.0
	0.0	0.0	0.1	0.0	0.1	0.0	0.0	0.0
	0.8	0.3	0.0	0.5	0.0	0.6	0.7	0.9
1	0.0	0.7	0.0	0.0	0.0	0.7	0.0	0.4
	0.0	0.0	0.4	0.0	0.8	0.8	0.8	0.7
Early	0.7	0.6	0.0	0.7	0.0	0.0	0.6	0.8
layers	0.0	0.0	0.0	0.6	0.0	0.7	0.1	0.5
	0.8	0.0	0.0	0.8	0.8	0.9	0.7	0.0
Attention heads								

## Figure 1: Visualization of gating scores

	Zero-shot					
	32K	128K	256K	512K	1M	
Infini-Transformer (L) Infini-Transformer (L + D)	14/13/98 13/11/99	11/14/100 6/9/99	6/3/100 7/5/99	6/7/99 6/8/97	8/6/98 7/6/97	
			FT (400 steps)			
Infini-Transformer (L) Infini-Transformer (L + D)	100/100/100 100/100/100	100/100/100 100/100/100	100/100/100 100/100/100	97/99/100 100/100/100	96/94/100 100/100/100	

Table 2: 1M passkey retrieval

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Model	Rouge-1	Rouge-2	Rouge-L	Overall
BART	36.4	7.6	15.3	16.2
BART + Unlimiformer	36.8	8.3	15.7	16.9
PRIMERA	38.6	7.2	15.6	16.3
PRIMERA + Unlimiformer	37.9	8.2	16.3	17.2
Infini-Transformers (Linear)	37.9	8.7	17.6	18.0
Infini-Transformers (Linear + Delta)	40.0	8.8	17.9	18.5

#### Table 3: 500k length book summary

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Thank You

# Q & A

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